

Superconductivity in MgB_2 and B-doped diamond

- two gap superconductivity in MgB_2

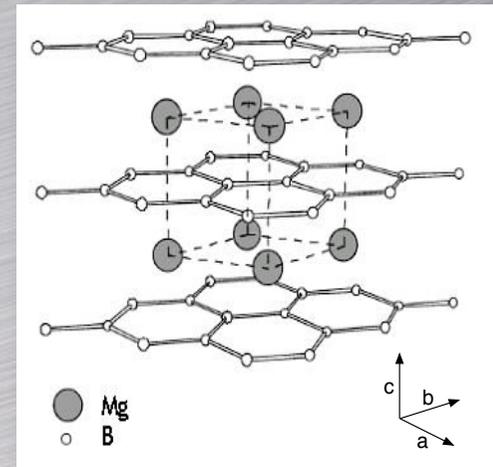
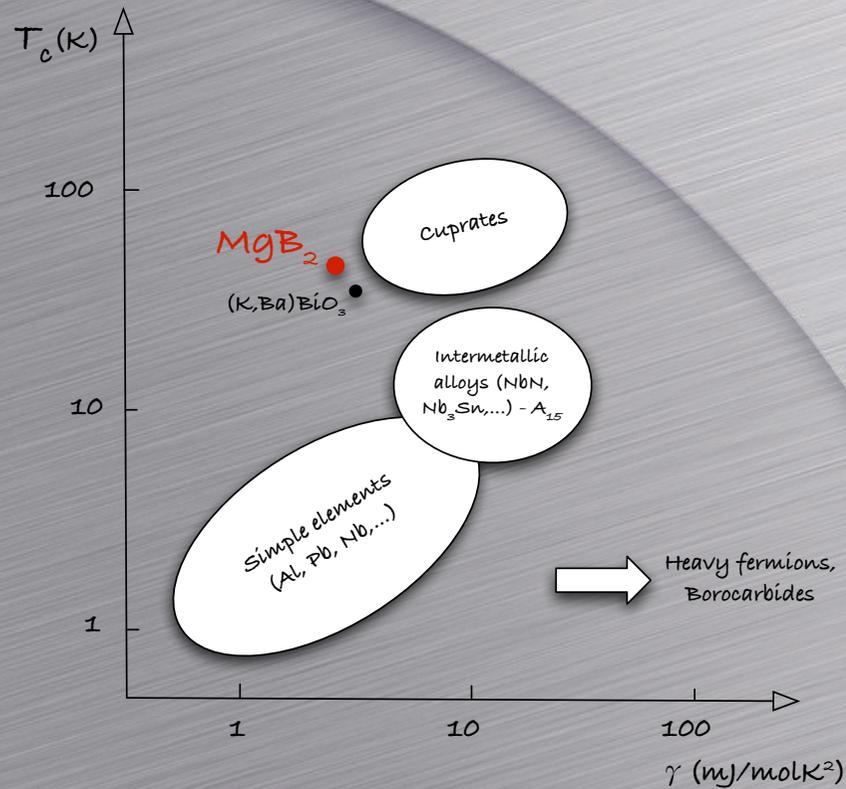
L.Lyard, C.Marcenat, J.Marcus

- superconductivity in B-doped diamond : proximity of a metal-insulator transition

E.Bustarret, E.Gheeraert, C.Marcenat, F.Gustafsson, J.Marcus

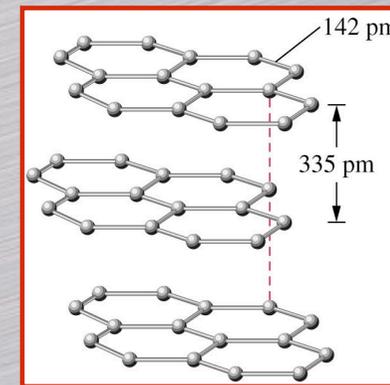
MgB₂ : a new "high T_c" superconductor

T_c ~ 40K

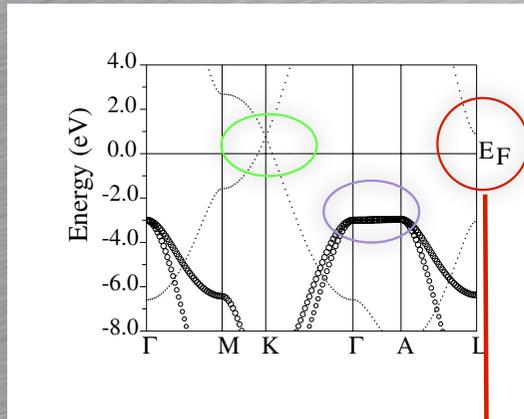
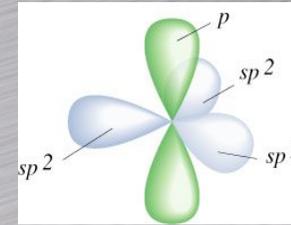


hexagonal structure

B planes similar to C planes in graphite

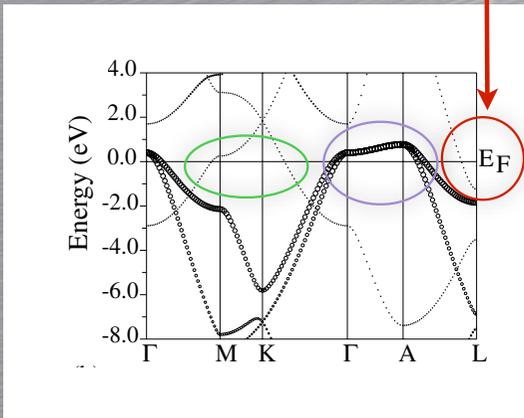


- 2 kinds of electronic orbitals derived from
- in plane sp_2 -boron orbitals : σ bands
 - p_z boron orbitals : π bands



“same” electronic structure than in Graphite
in which the σ bands are full
(involved in covalent bounds)

→ π band : small e/hole pockets close to the K point



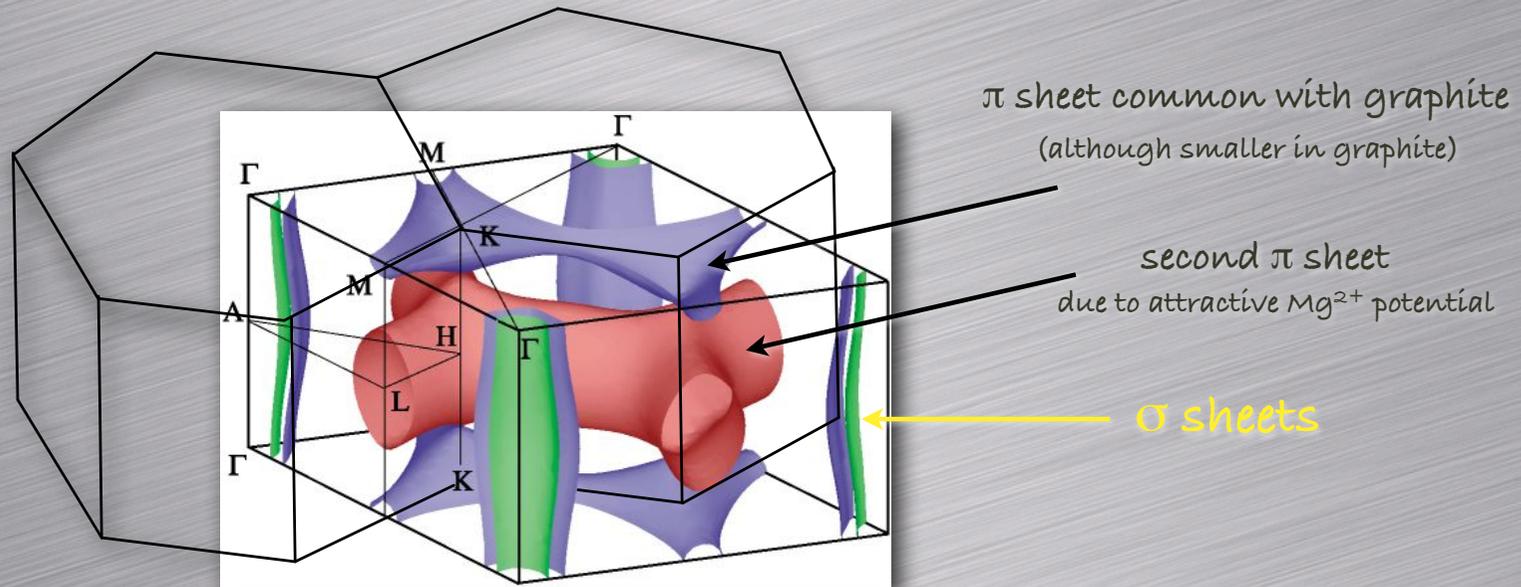
in MgB_2 the “second” π band is lowered
by attractive Mg^{2+} potential

charge transfert from σ to π bands

→ unfilled σ bands

"2" Fermi surface sheets

actually $2 \times \pi$ (3D) and $2 \times \sigma$ (quasi-2D) bands



the quasi 2D characters leads to a "large" DOS ~ 0.30 st/eV.cell

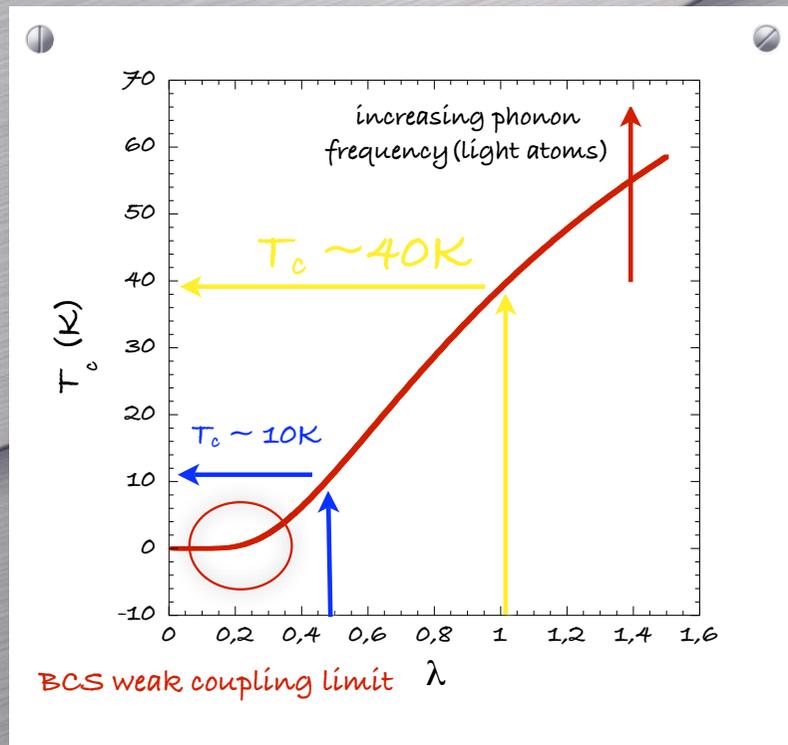
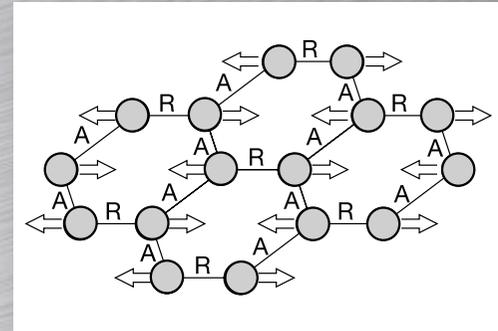
(close to the 2D value $m^* a^2 / \pi \hbar^2 \sim 0.33$ st/eV.cell)

despite the small hole doping level ~ 0.07 hole/B

strong coupling of σ electrons with E_{2g} vibration mode
+ large DOS

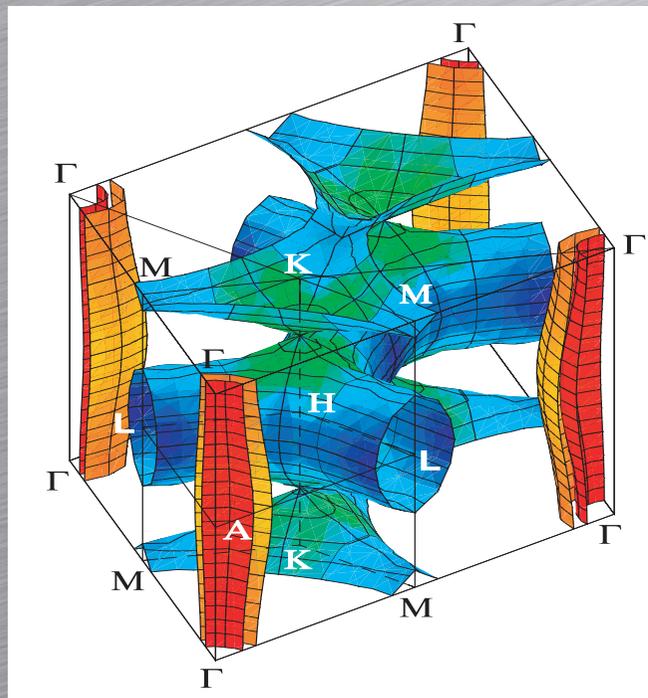
-> electron-phonon coupling constant $\lambda \sim 1.0$

despite a larger DOS ($\sim 0.4 \text{st/ev.cell}$)
the coupling is much worse in the π band ; $\lambda \sim 0.45$

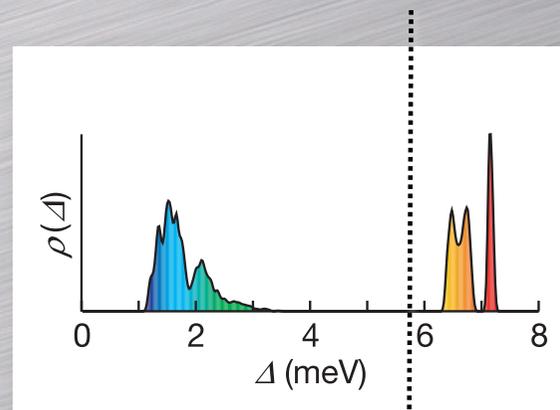


Mac-Millan expansion
screening coefficient : 0.15
 $\omega = 540\text{K}$

Two co-existing superconductors ????

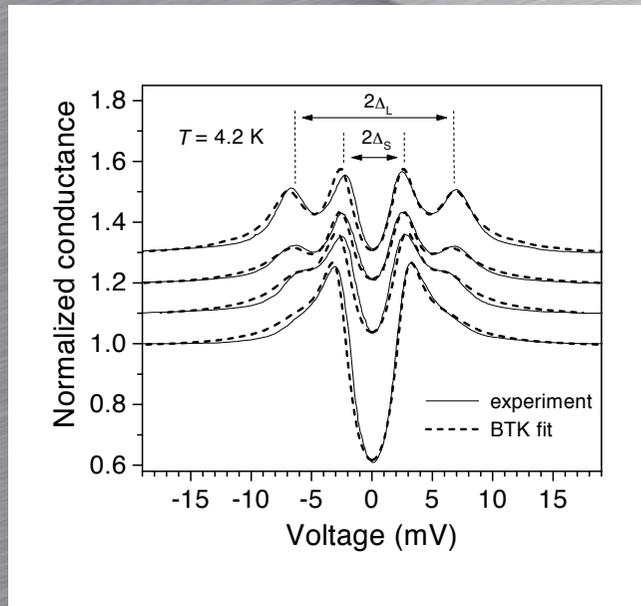


2 SF sheets \longrightarrow 2 gaps



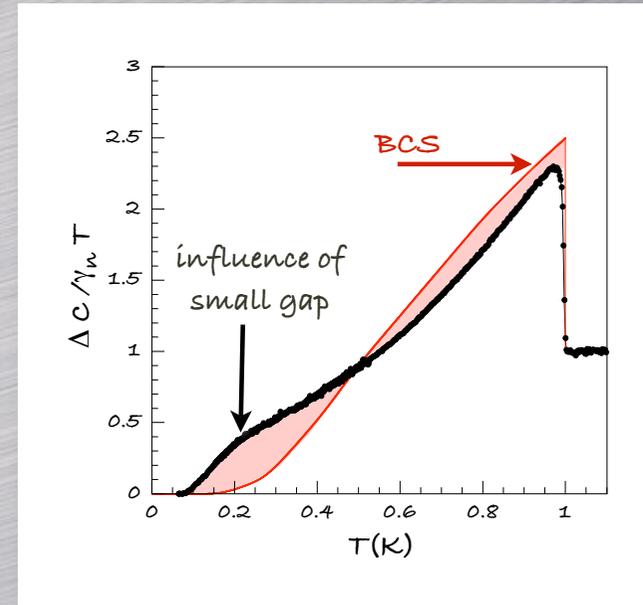
BCS value

point contact spectroscopy



P.Szabo et al. PRL 01

confirmed by specific heat (i.e. bulk) measurements

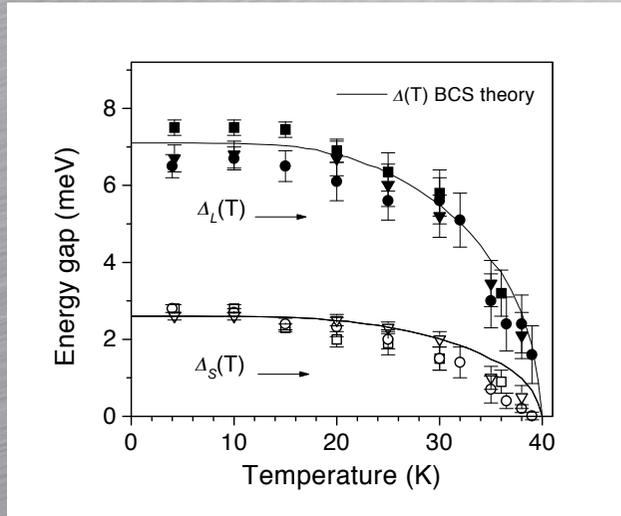


see also F.Bouquet et al. EPL 01

$$C_p/T : \gamma \propto e^{-\Delta/kT}$$

2 gaps => 2 T_c values ???

but present different field dependences

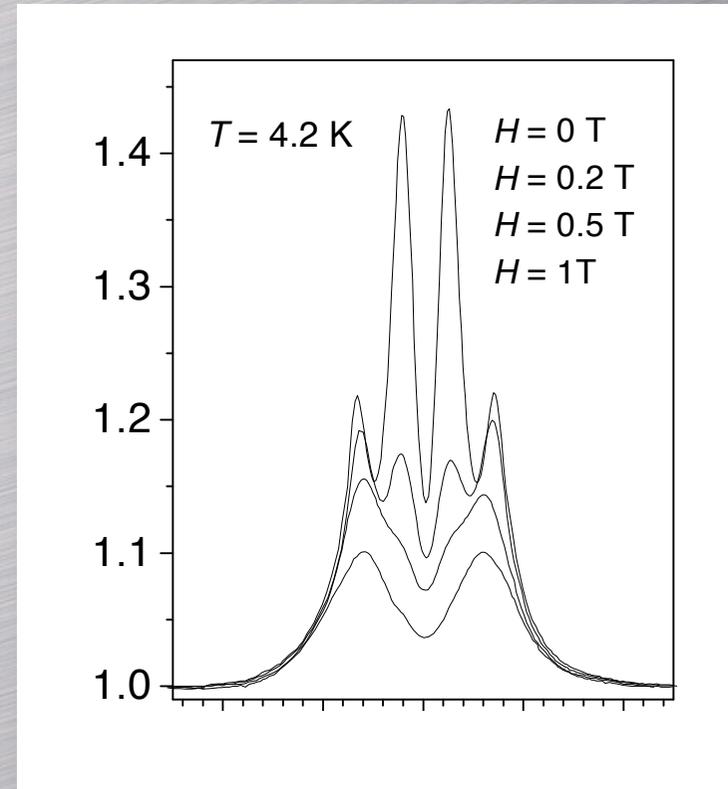


both gaps are closing at the **same T_c**
 \Rightarrow weakly coupled bands



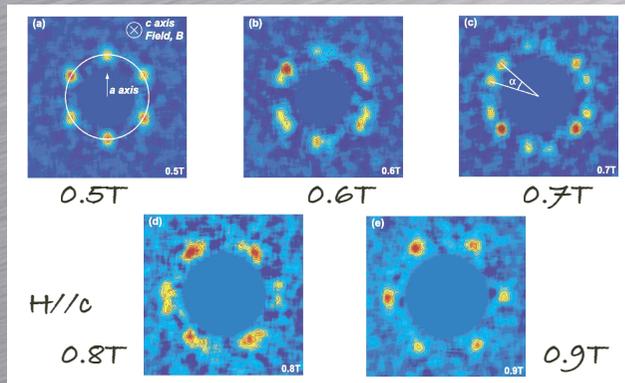
zero coupling
 $\Rightarrow 2 T_c$'s

strong coupling
 \Rightarrow FS averaged
 λ value (~ 0.7)
 $\Rightarrow T_c \sim 20$ K



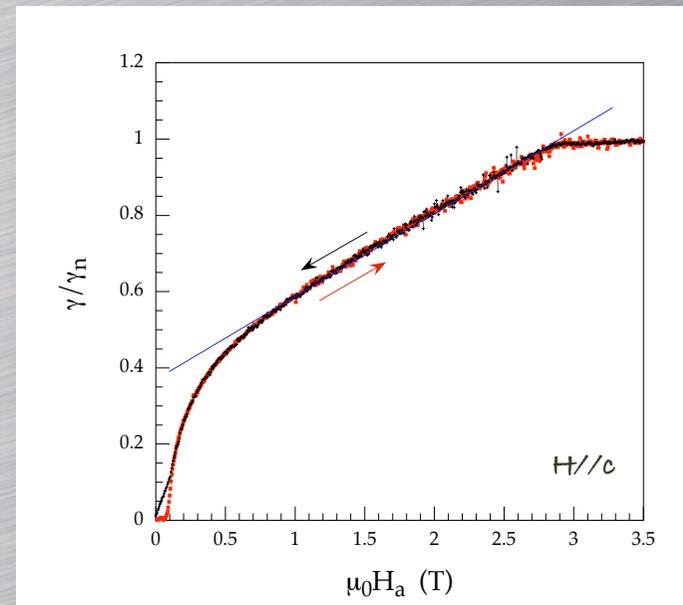
the small gap is very sensitive to H i.e.
 "disappears" around 1 T

and the vortex lattice
rotates by 30°



SANS measurements R.Cubitt et al. PRL 03

+ anomalous field dependence of γ

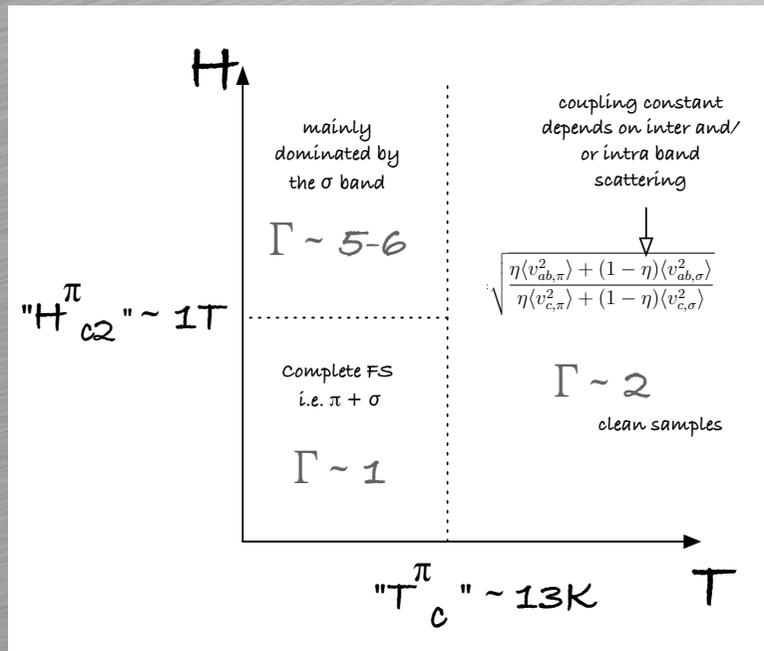


see also F.Bouquet et al. PRL 02

Should the system be described by two ξ and two λ values (associated with each band) or only one field dependent value (as we believe)?
In any case the "properties" of the superconducting state are going to be strongly field dependent: *exemple of the anisotropy*

$$\Gamma = \frac{\langle m_{ab}^* \rangle_{FS}}{\langle m_c^* \rangle_{FS}} = \sqrt{\frac{\langle v_{F,c}^2 \rangle_{FS}}{\langle v_{F,ab}^2 \rangle_{FS}}} = \frac{\lambda_c}{\lambda_{ab}} = \frac{\xi_{ab}}{\xi_c}$$

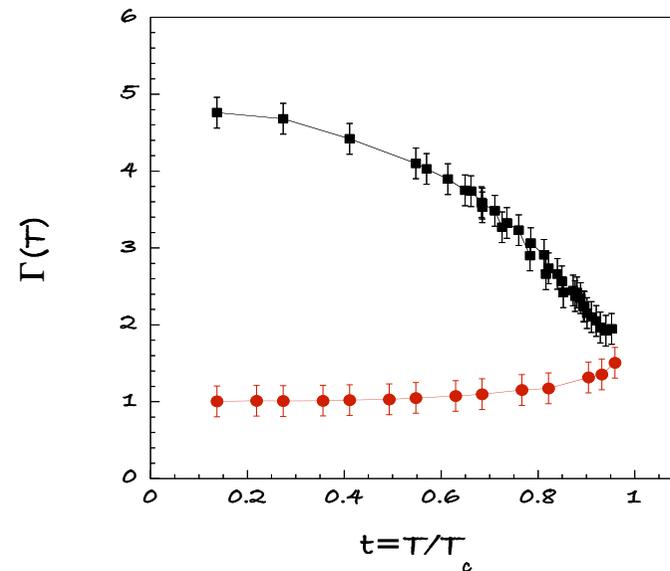
Which Fermi Surface should we take into account ???



How can we get Γ ???

high field: $\Gamma = \Gamma_{H_{c2}} = \frac{H_{c2,ab}}{H_{c2,c}}$

low field: $\Gamma \sim \Gamma_{H_{c1}} = \frac{H_{c1,c}}{H_{c1,ab}}$



from C_p and magnetotransport, Lyard et al. PRB 02

from C_p and Hall probe magnetometry, Lyard et al. PRL 04

what about Graphite.....

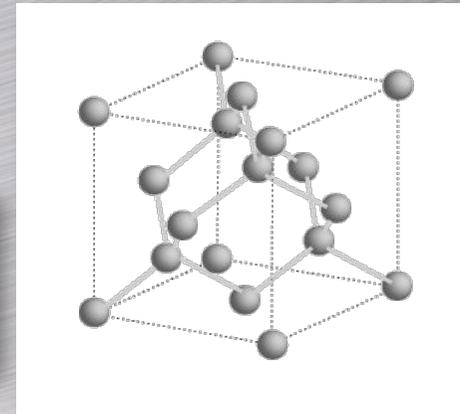
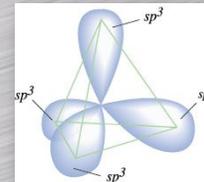
doping by intercalation (Na,...) leads to
superconductivity : $T_c \sim 5K$

but superconductivity
remains in the "soft" π band
(similar to alkali doped fullerenes)



DIAMOND
very "strong" σ bounds

but 3D (sp^3).....



Superconductivity ($T_c \sim 7K$) has been
observed in Ba doped Si-clathrates
(cage like structure with sp^3 bounds)

all 4e are involved in covalent bounds -> large gap semiconductor

can be either n or p doped by substituting C atoms by P or B atoms, respectively

In B-doped samples, the system becomes **metallic** when the boron impurity band overlaps the diamond valence band
i.e. for boron concentrations > a few 10^{20} cm^{-3}

what about the e-phonon coupling λ ???

$$\lambda = N(E_F) \cdot \frac{I^2}{M\omega^2}$$

DOS
st/ev.spin."2 atoms-cell"

FS averaged e-ion
matrix element

"appropriately defined"
mean square frequency

$\pm u$: splitting of the top of the valence band
for the "appropriate" displacement u

	N	I (eV/A)	$\omega(\text{cm}^{-1})$	$I^2/M\omega^2$	λ
MgB ₂	0.15	12	540	6.7	1.0
C-B3%	0.06±0.01	24±3	1080	7.5±0.8	0.45±0.1

2x the already large
MgB₂ value

1/2 of MgB₂ value to
smaller DOS (3D)

	method	model	B/C at.%	n_B 10^{20} cm^{-3}	e/ph coupling λ	T_c (K)	Remark
Boeri et al PRL 93, 237002	First Principles LMTD	VCA Virtual crystal	3	50	0.37	0.2	$T_c = 25 \text{ K}$ for 10 at%
Lee et al PRL 93, 237003	First principles APW-CPA	VCA Virtual crystal	2.5	44	0.53	9	E_F at VBM ^u -0.6eV
Xiang et al Cond-mat 0406446	First principles supercell DFT-LDA	$C_{35}B$	2.8	49	0.39	4.4	B modes contribute to e/ph coupling
Blase et al PRL 93, 237004	Ab initio Supercell DFT-LDA	$C_{53}B$	1.85	33	0.43	4	« Local » C-B modes couple with free carriers E_F at -0.52eV

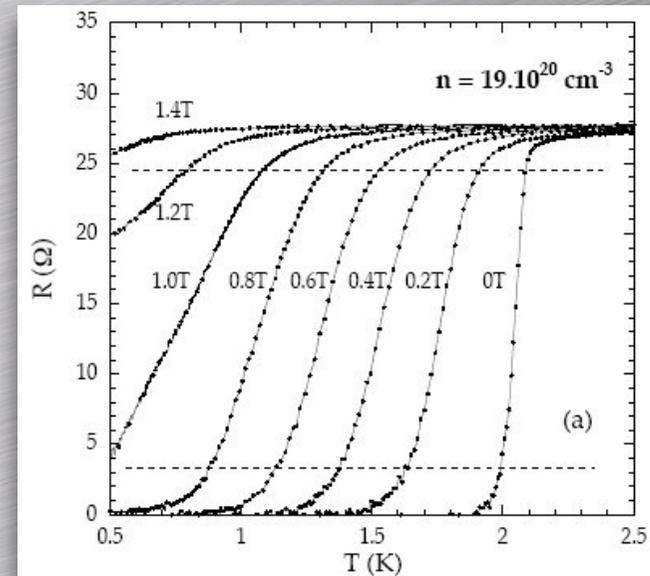
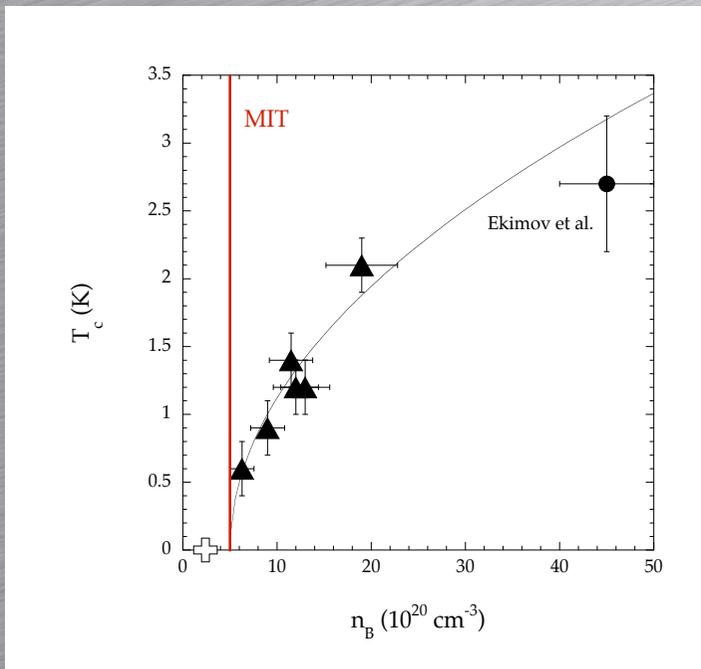
phonon modes involved in e/ph
coupling not clearly identified

Ekimov et al. Nature 04

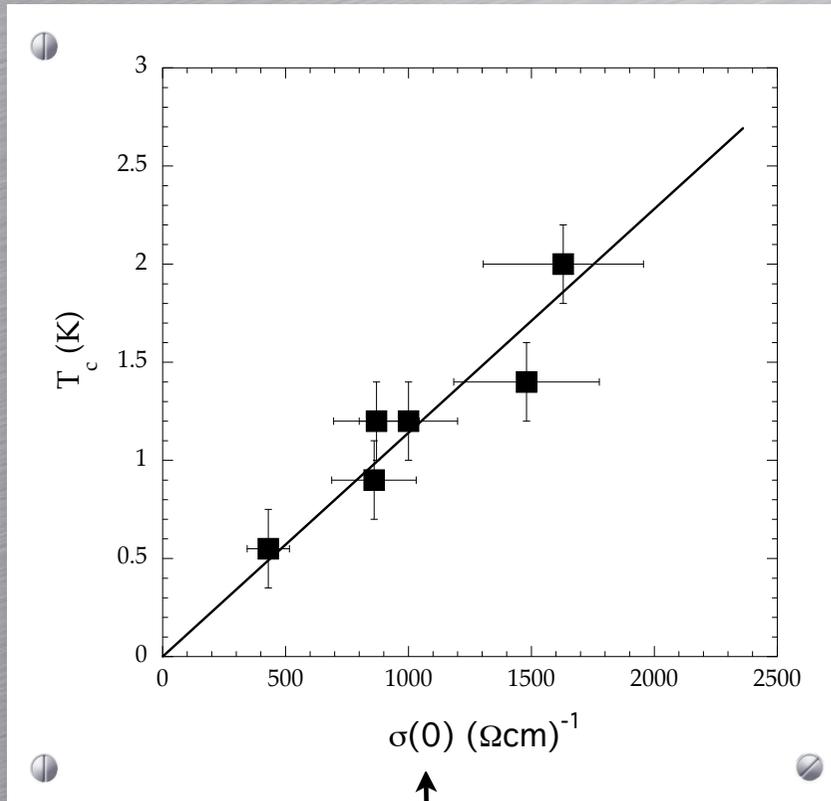
- Polycrystalline diamond (HPHT bulk)
- Doping level : 10^{21} B/cm³ : $T_c \sim 3K$

confirmed on homoepitaxial films

E. Bustarret 04



is there any relation between this metal-insulator transition and superconductivity ???



$$T_c \sim \sigma(0) ???$$

enhanced superconductivity
due to reduced screening close
to the MIT ???

Soulen - Osofsky et al.

normal state conductivity extrapolated to zero

Hole doping of the σ bands leads to very efficient electron-phonon interaction potential

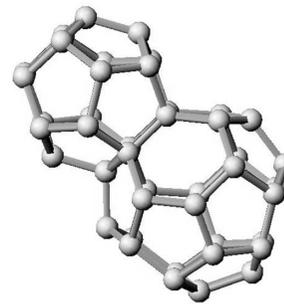
+ large DOS due to 2D character (sp^2) in MgB_2
 $\Rightarrow T_c \sim 40K$

superconducting is also "induced" in the π band
 \rightarrow two gap superconductivity

anomalous field and temperature dependence of the superconducting properties

can explain the onset of superconductivity in B-doped diamond in, which "reduced" DOS $\Rightarrow T_c \sim$ a few K

superconductivity appears in the vicinity of a MIT



large T_c values predicted in C clathrates ($X_8@C_{46}$)

$\lambda \sim 1.4$ $\xi \omega \sim 1500K$

$\Rightarrow T_c$ between 50

and ...150K !!!

(depending on screening coefficient)

Connetable et al. 2003